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Warsaw, POLAND



Carbon atomic structures promoting twisted growth of second Graphene layer at magic angles 21.78° and 27.8° .

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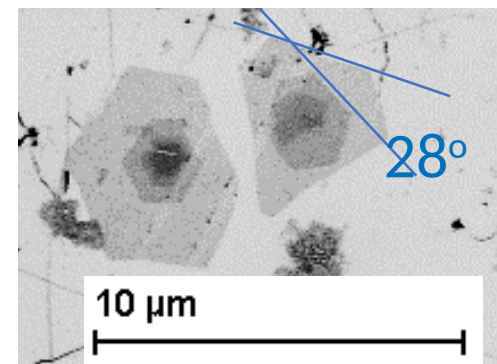
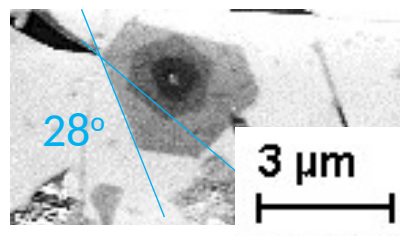
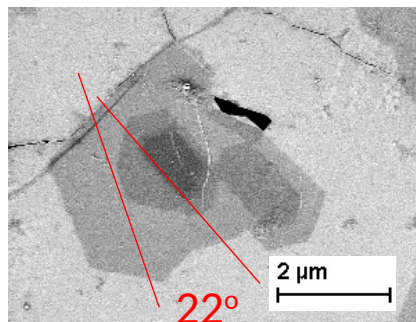
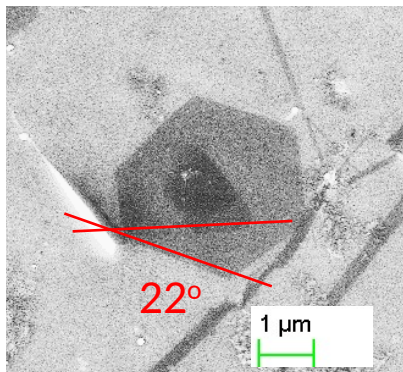
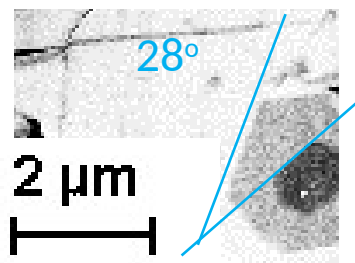
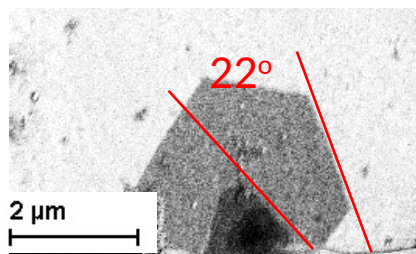
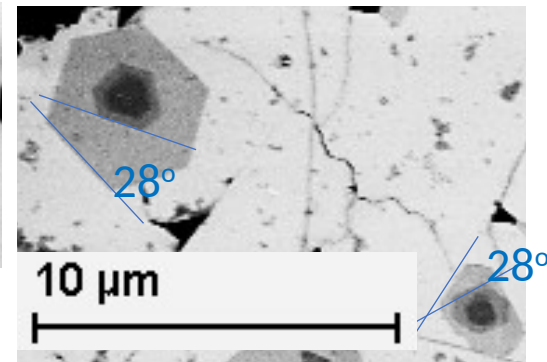
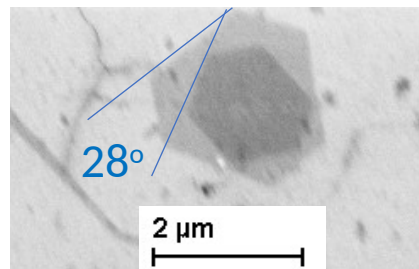
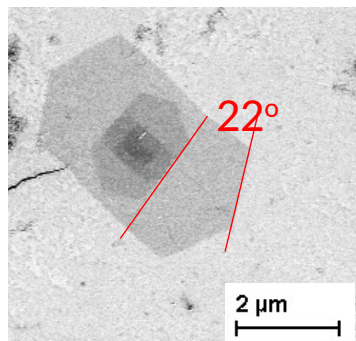
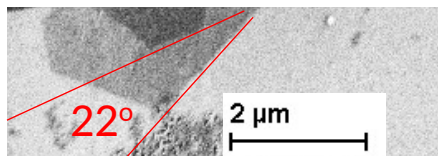
a) Institute of Electronic Materials Technology. POLAND

b) National Centre for Nuclear Research. POLAND.

Turbostratic Graphene multilayer islands twisted at $\sim 22^\circ$ & $\sim 28^\circ$

Observations

SEM micrographs



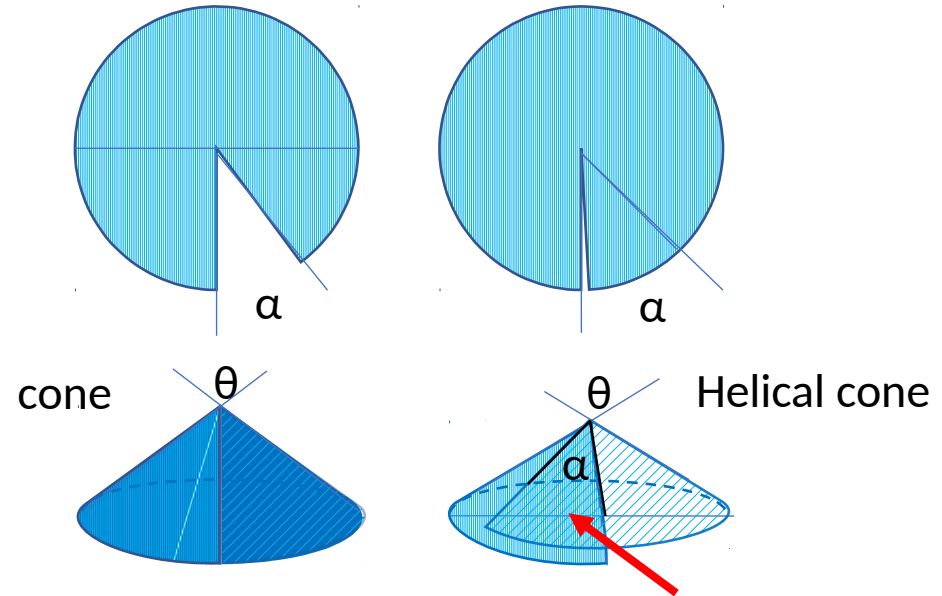
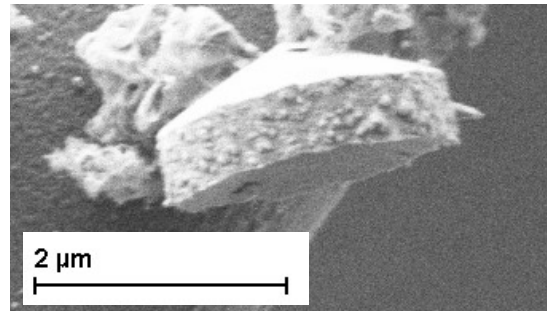
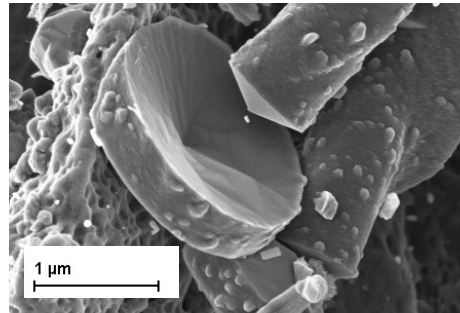
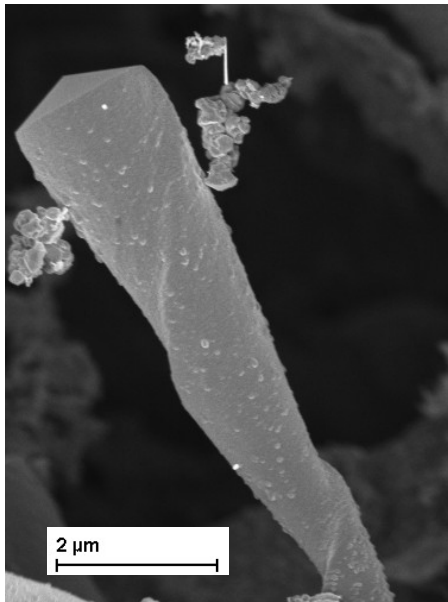
CVD Graphene grown on Cu foil and then transferred onto a glass substrate

Magic angles in Conical Graphene structures of biographene

Raman spectrum of natural Graphene whisker

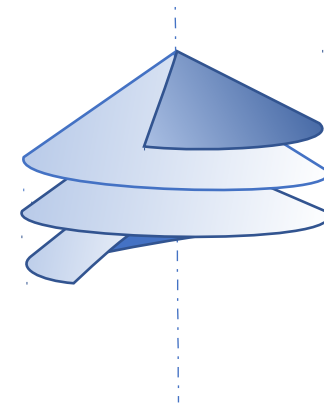


Graphene structures from natural biomaterials



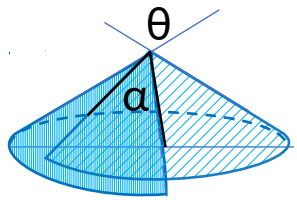
Bilayer twisted at angle α

$$\Theta = 2 \times \arcsin(1 - \alpha/360)$$

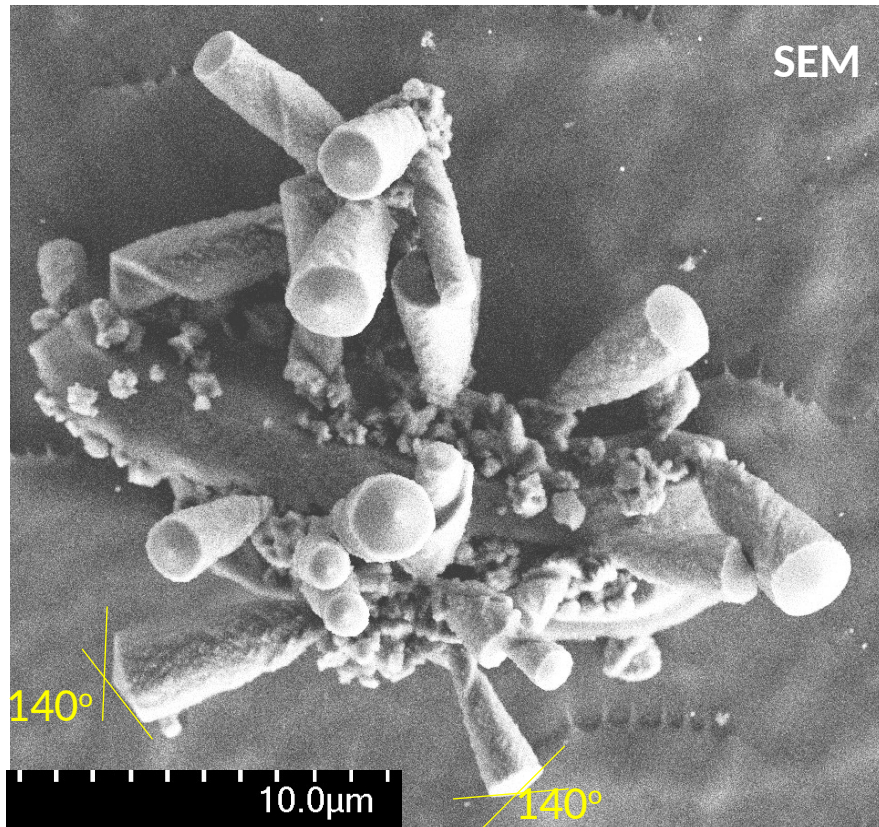


Whisker from helical cone

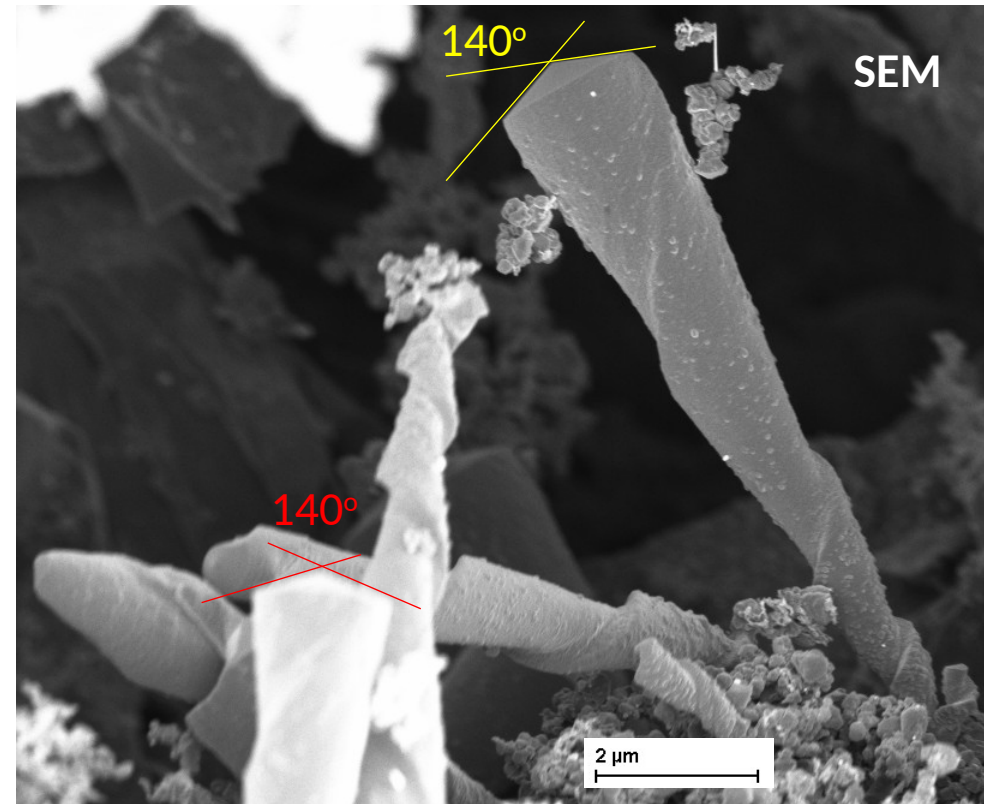
Graphene structures from natural biomaterials



Cone angle $\theta = 140^\circ$: Twist angle $\alpha = \sim 21.78^\circ$



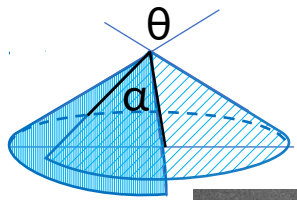
Dung Beetle leg



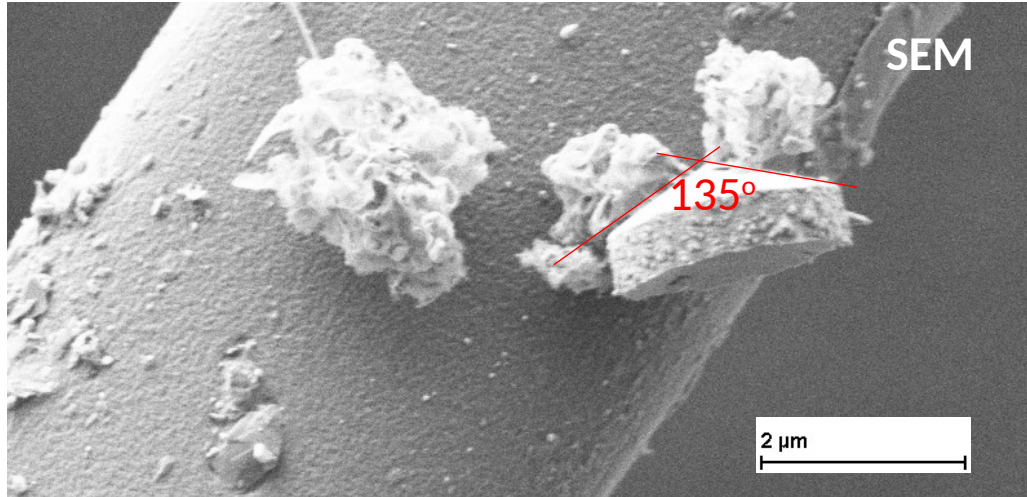
Anturium leaf

The same cone angles for different materials

Graphene structures from natural biomaterials

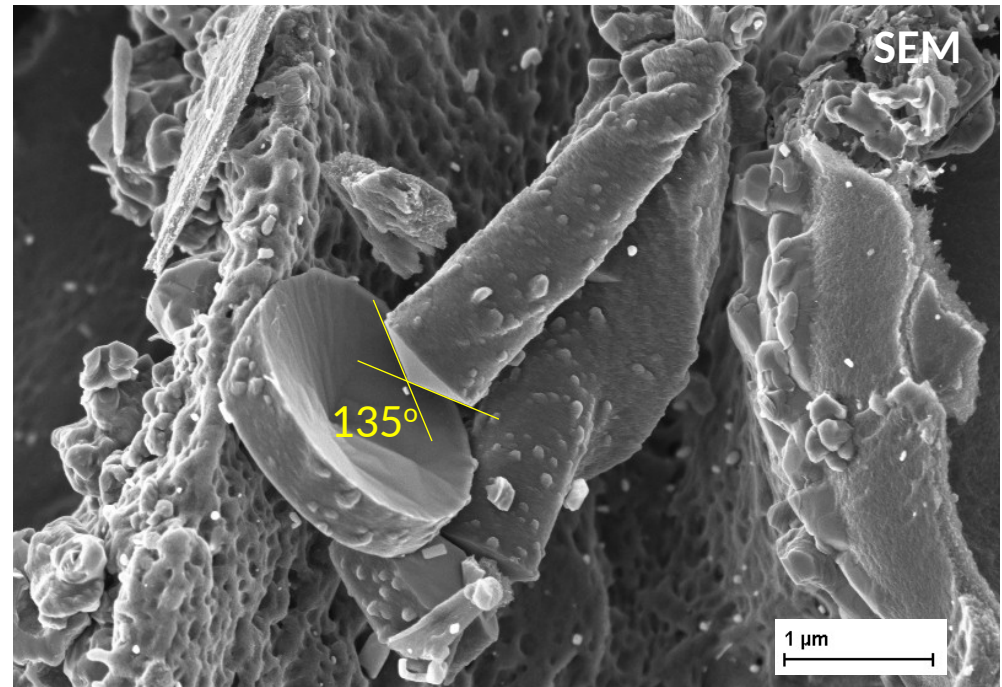


Cone angle $\theta = 135^\circ$: Twist angle $\alpha = \sim 27.8^\circ$



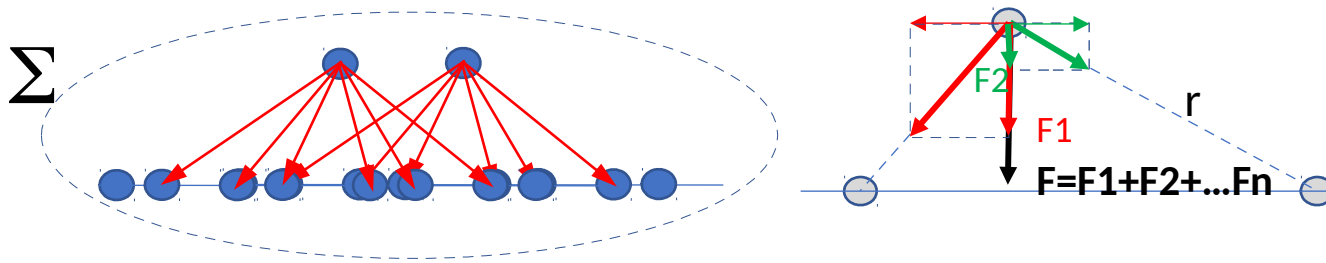
silk

Repeatedly constant cone angles
of 140° and 135°

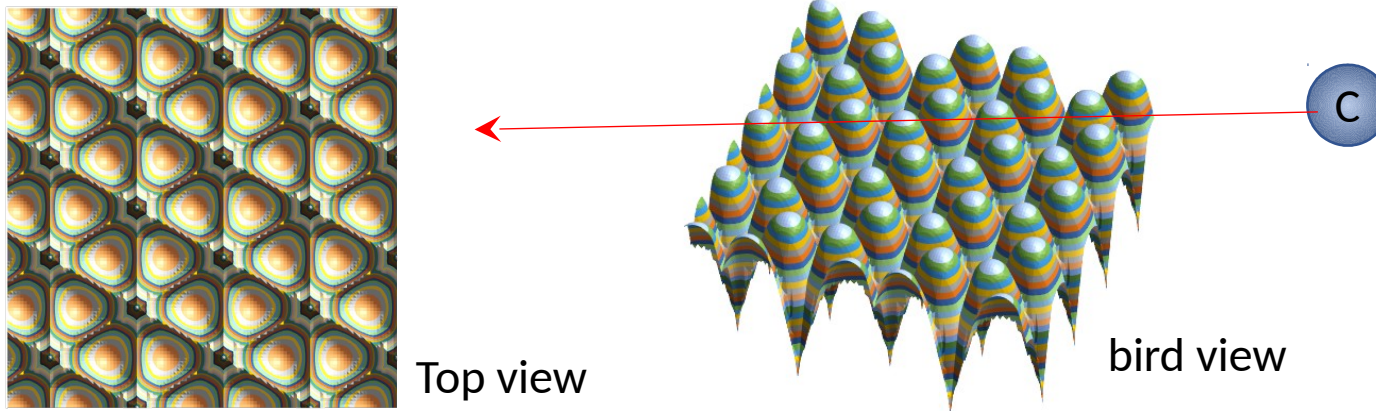


morning glory seed

1. **LAMPS** simulation with using Kolmogorov and Crispy potential (K-C) [*]
2. **Summarization** of attractive forces F normal to the Graphene plane acting on every carbon atom of the second layer by all atoms of the first Graphene layer ($\sim 1/r^7$)



Calculated landscape of normal attractive force acting on carbon atom moving over Graphene



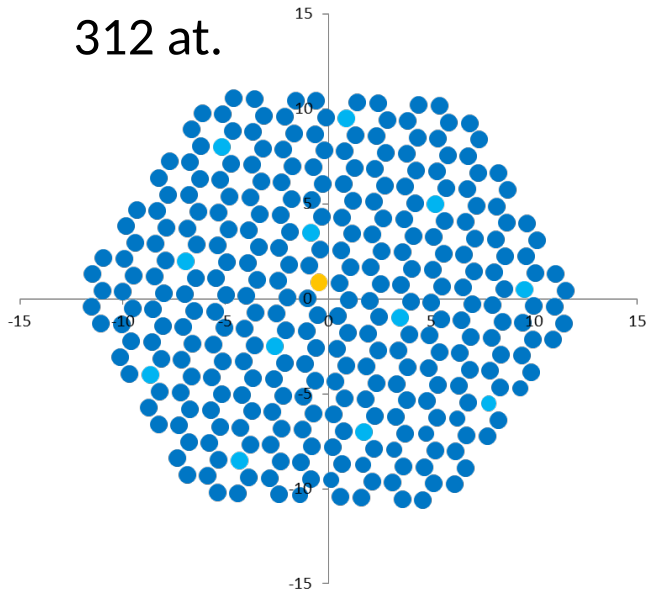
Position of rotation axis

- Three basically different positions of rotation axis
- Stable AB configuration
- Unstable AA stacking

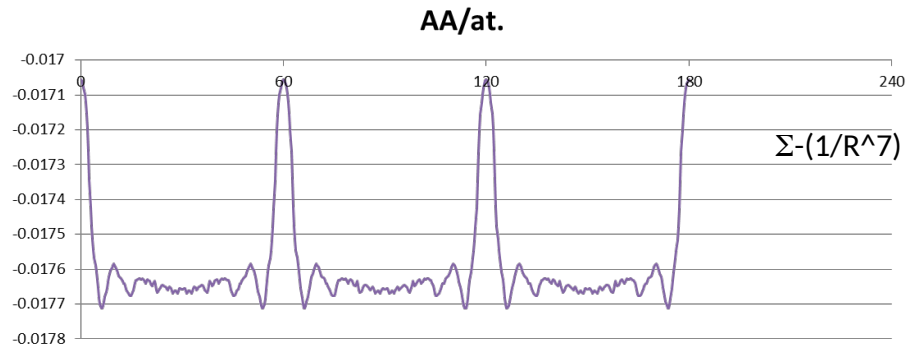
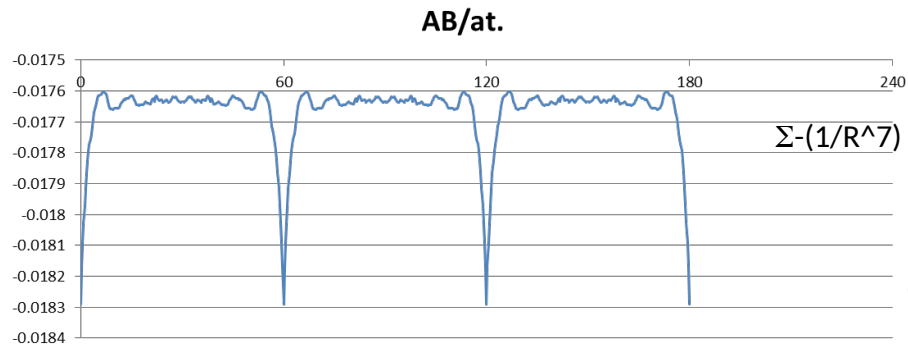
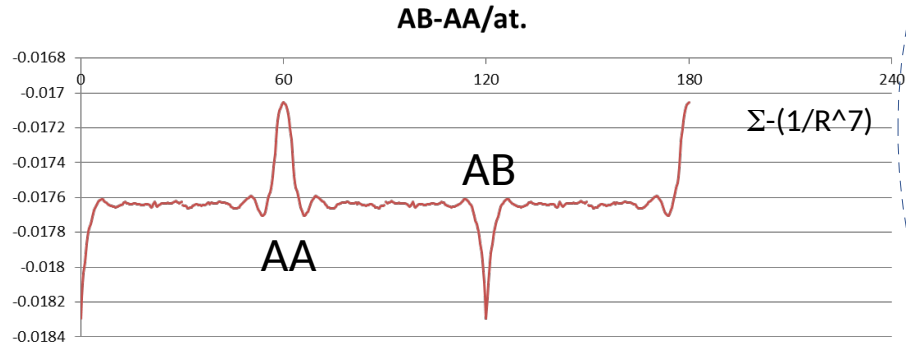
Simulated rotation of
group of 312 atoms



312 at.

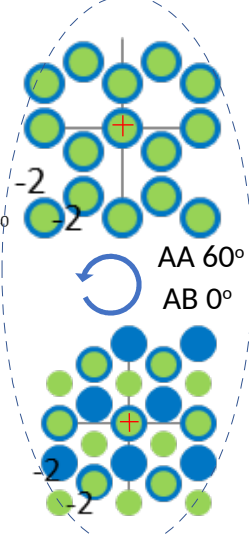


Attractive force

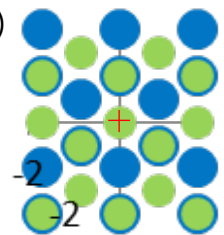


angle

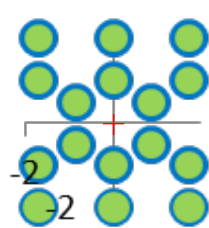
AA-AB-AA



AB-AB



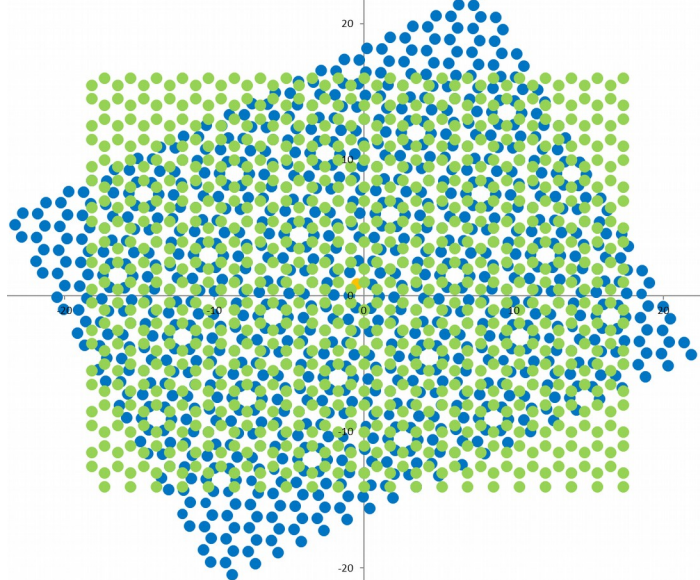
AA-AA



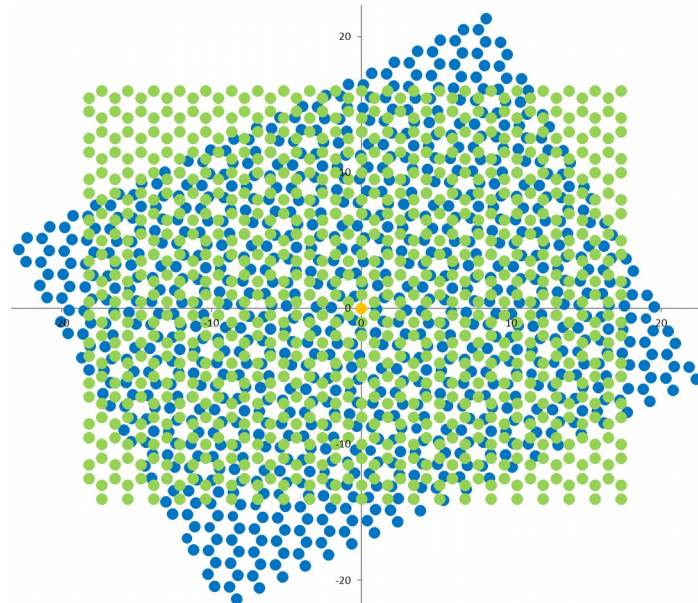
Moire patterns of twisted graphene bilayer

27.8°

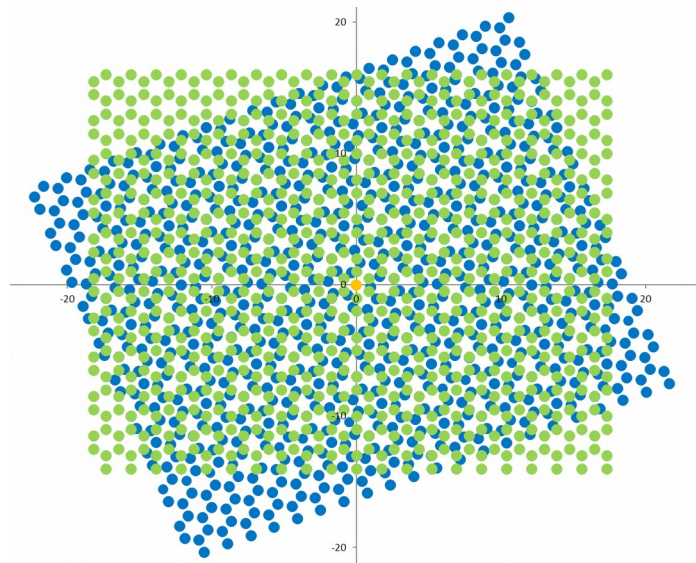
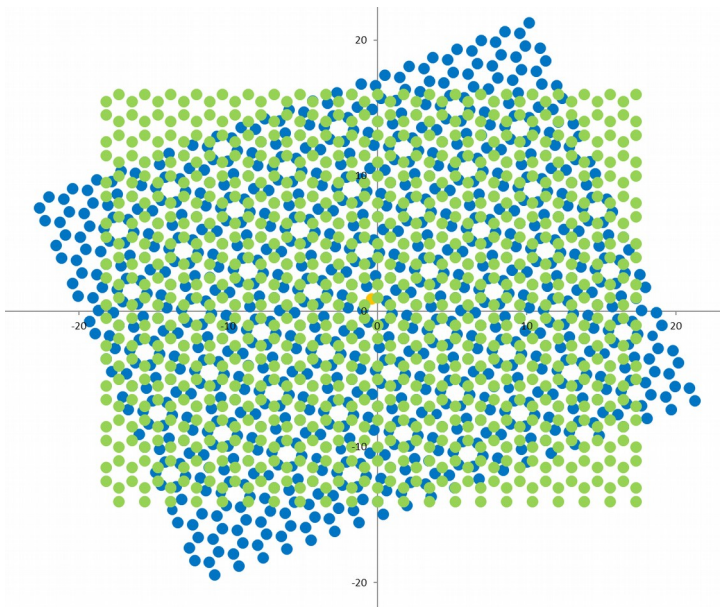
AA-AA



AB-AB



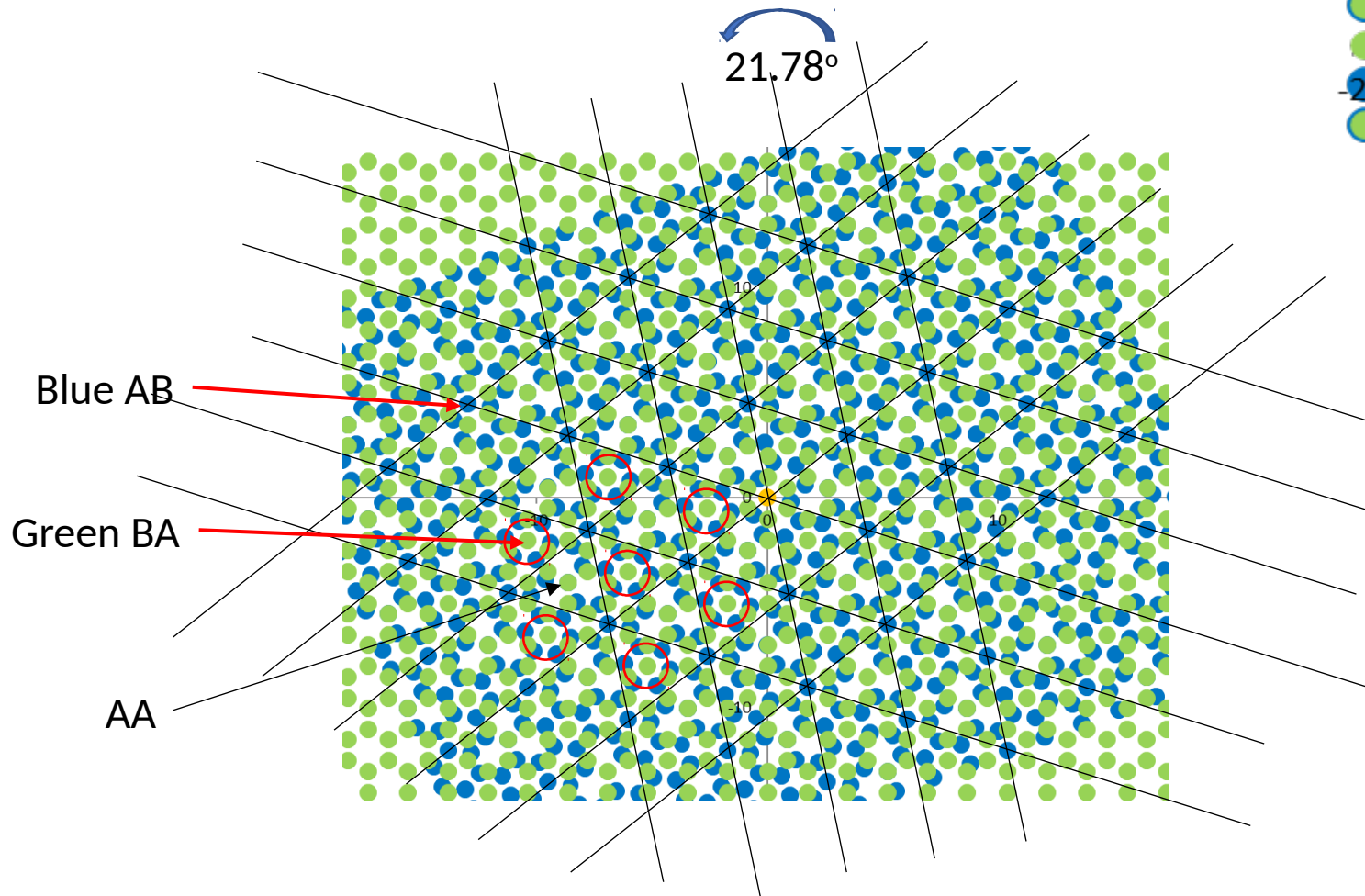
21.78°



AB-AB rotation at 21.78°

- No distinct impressive Moire pattern visible
- Some atoms are located on stable AB or BA positions
- There is a periodical network of atoms at stable positions

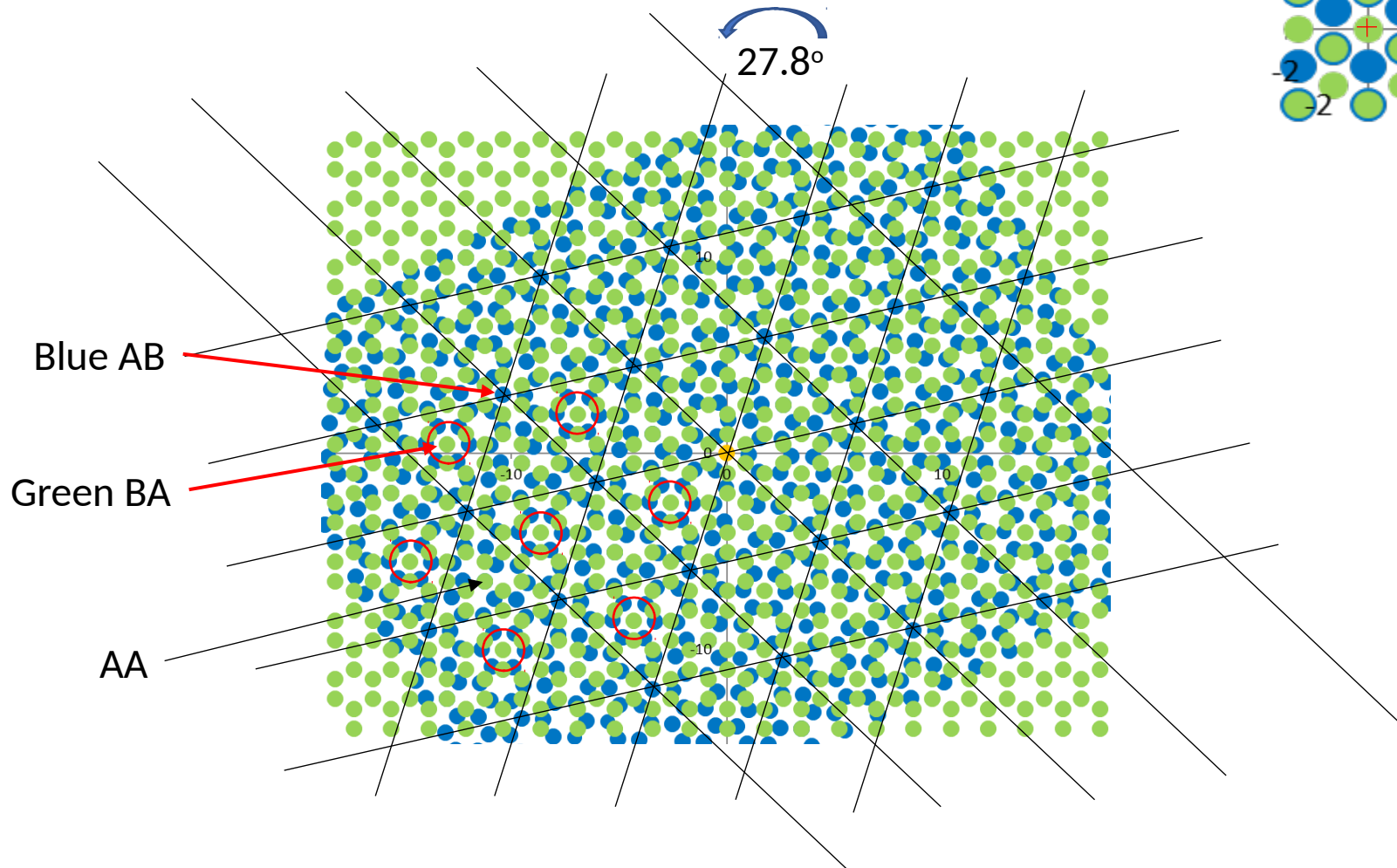
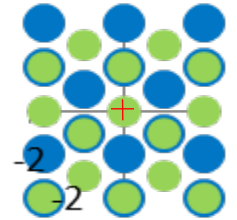
AB-AB rotation
axis position



AB-AB rotation at 27.8°

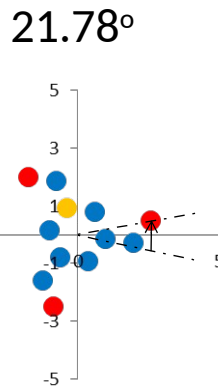
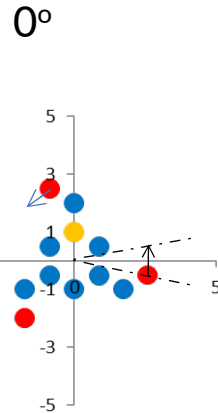
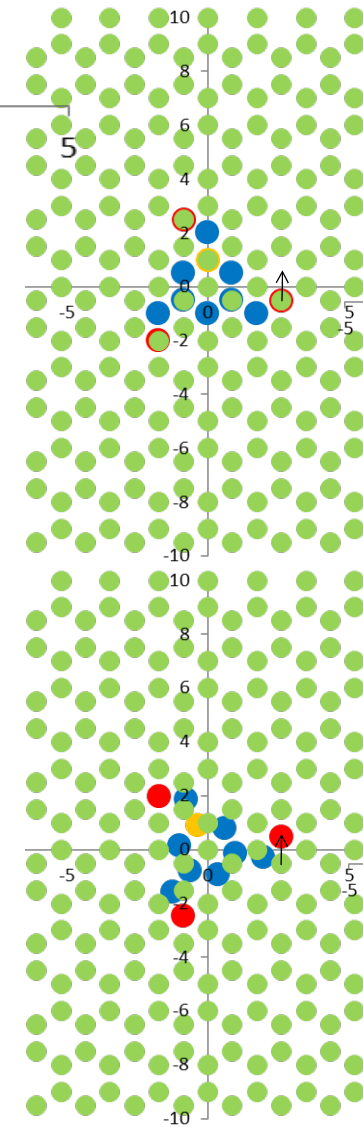
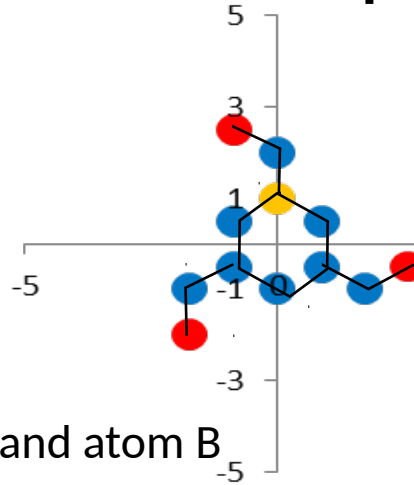
- Geometry very similar as for 21.78°
 - No distinct impressive Moire pattern visible
 - Some atoms are located on stable AB or BA positions
 - There is a periodical network of atoms at stable positions

AB-AB rotation
axis position

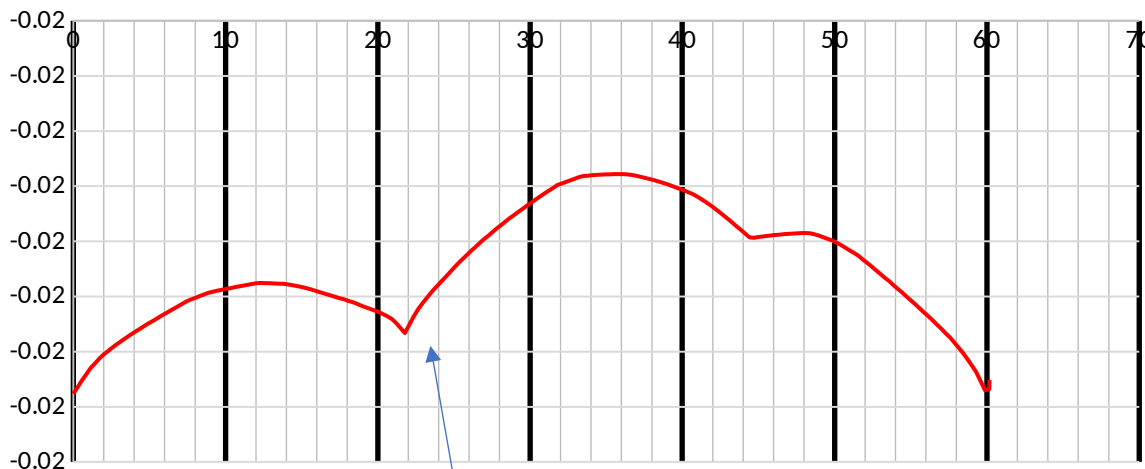


The basic structure with metastable position at 21.78° (AB)

- Initial configuration AB
- Rotation around center of hexagon A and atom B
- „RED” atoms stabilize rotation at 21.78° .
- There is 120° symmetry of the rotation of such structure



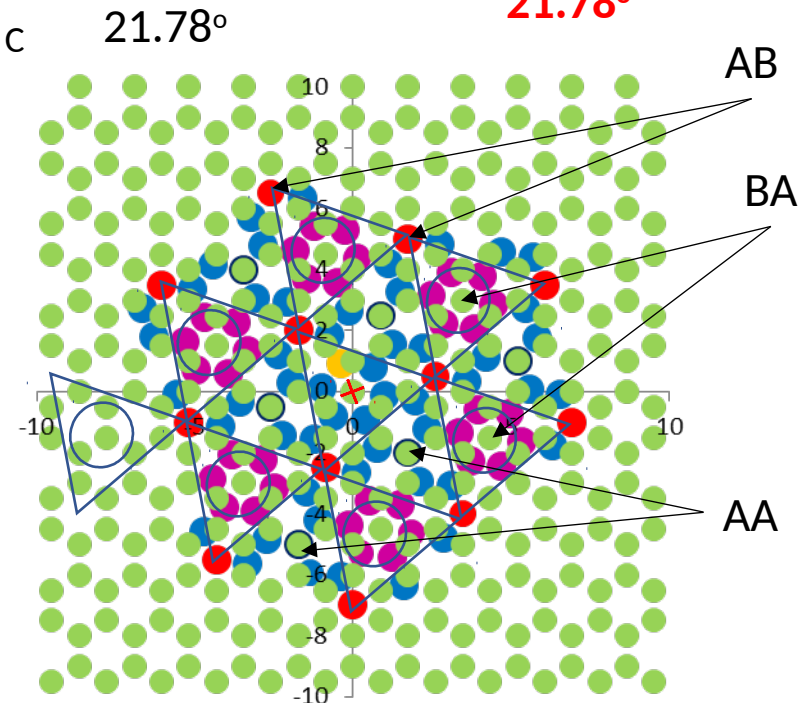
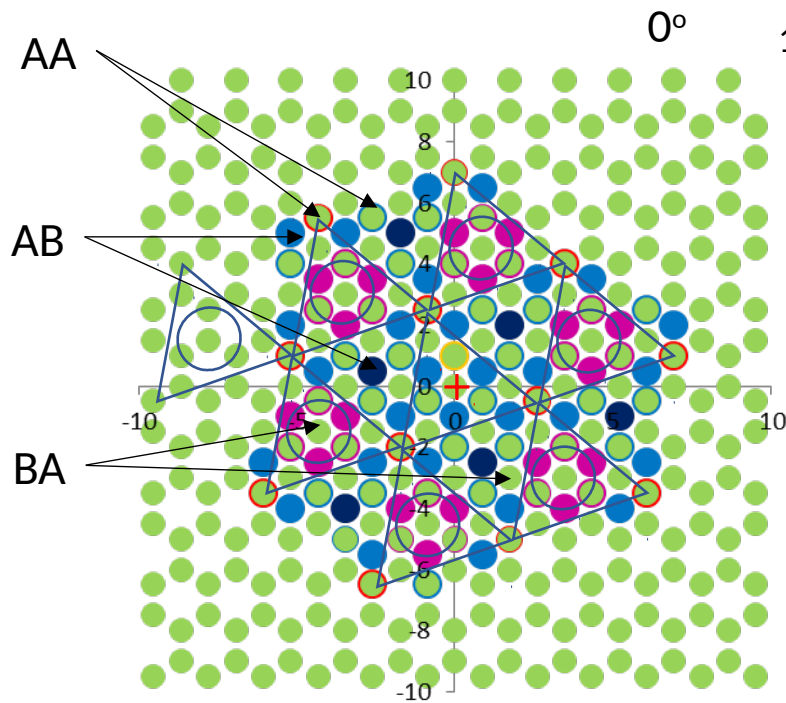
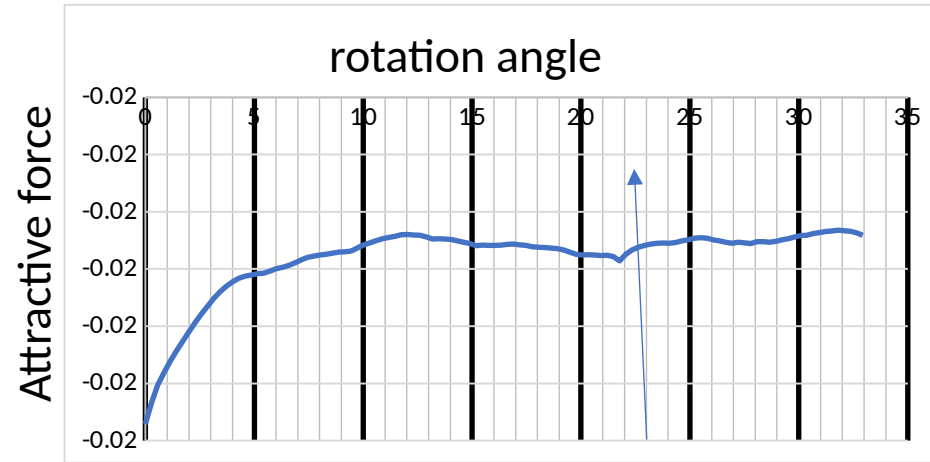
Attractive force vs. rotation angle



Metastable 21.78°

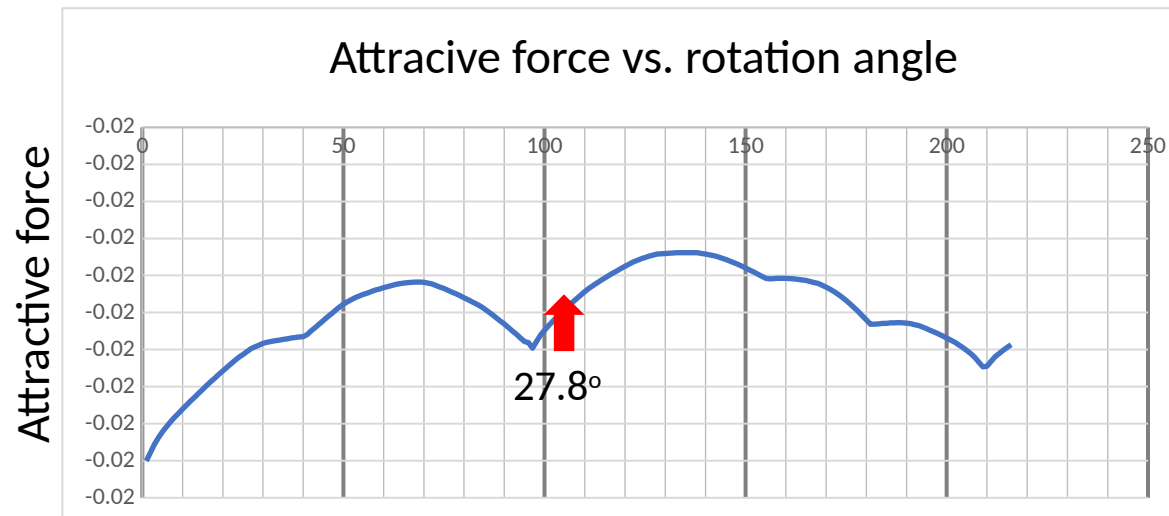
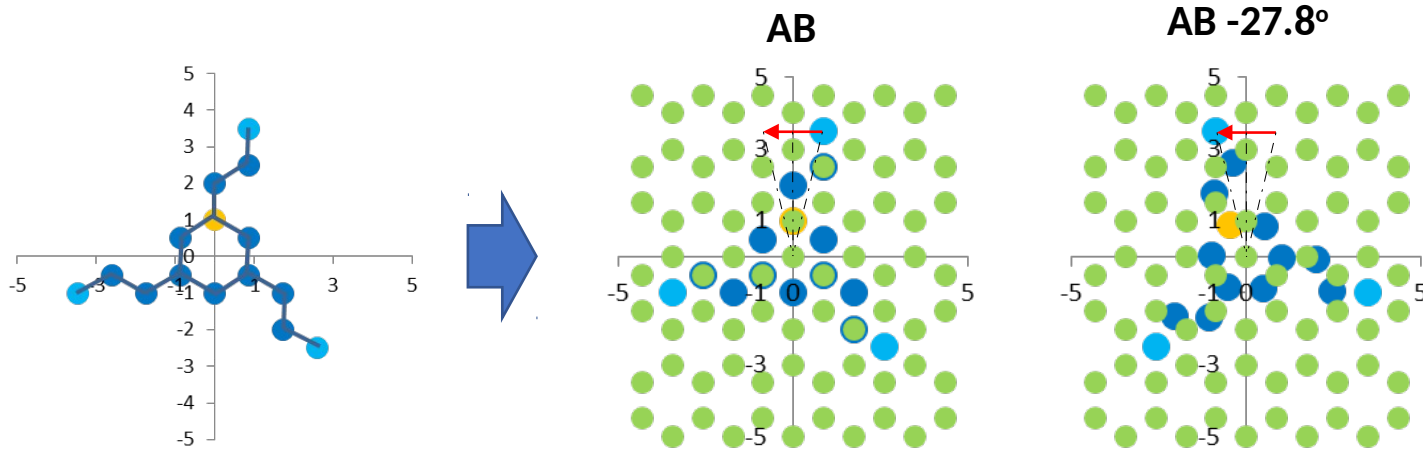
Bigger group of atoms (107 at.) at 21.78° (AB)

- Still metastable at 21.78°
- Diminishing of metastability with island growth

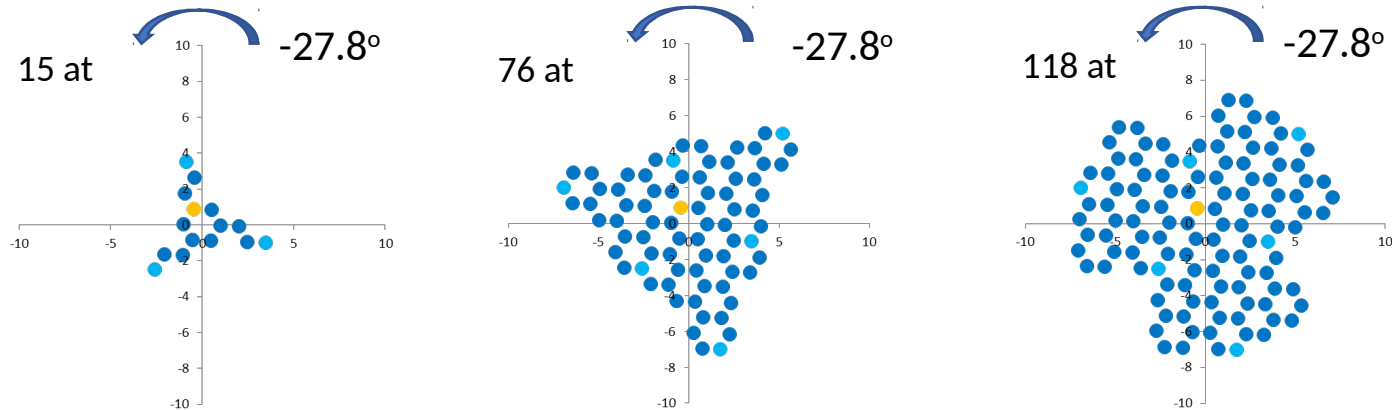


The basic structure with metastable position at 27.8° (AB) 15 atoms

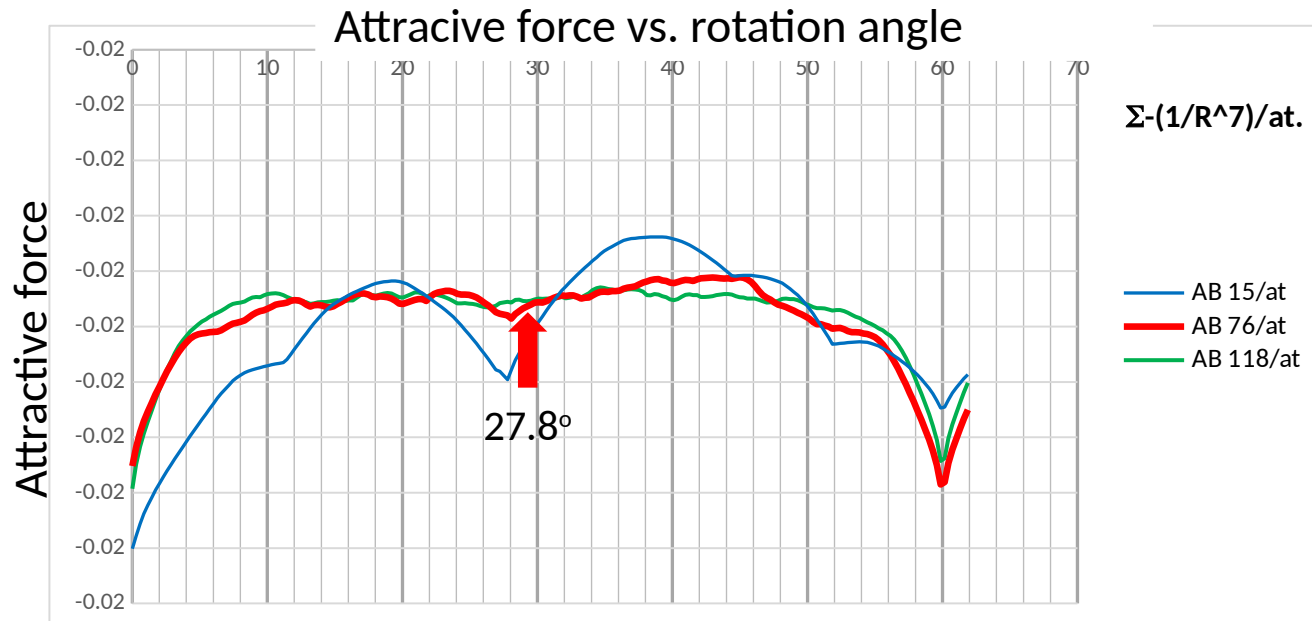
- Initial configuration AB
- Rotation around center of hexagon A and atom B
- There is 120° symmetry of the rotation



Metastability changes with island growth

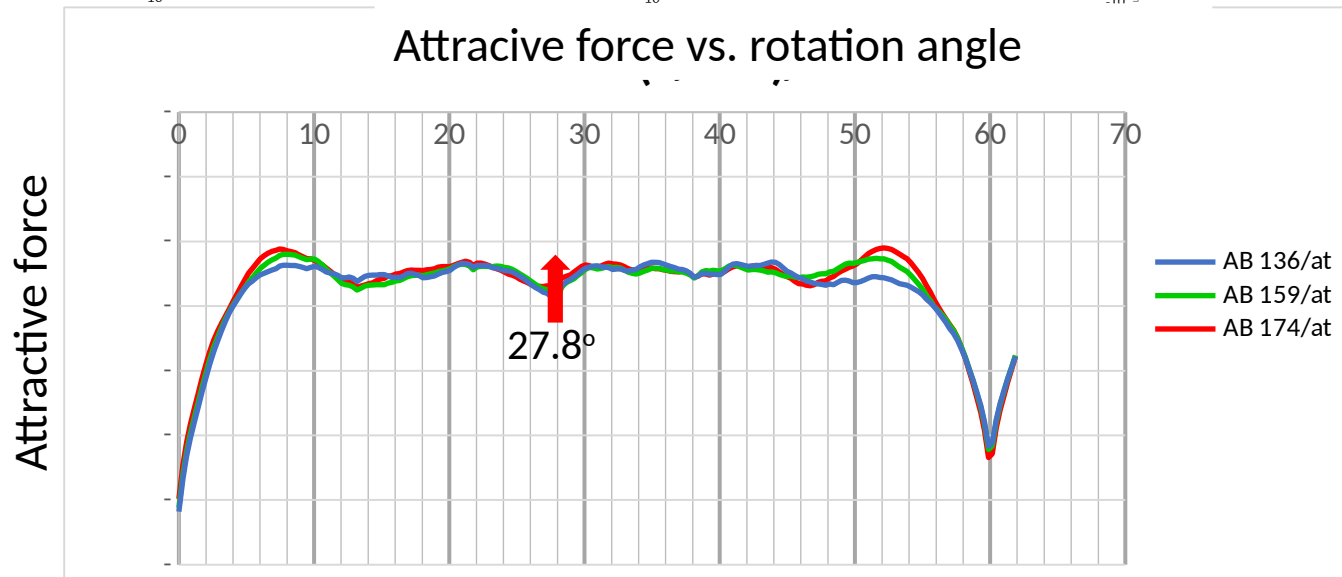
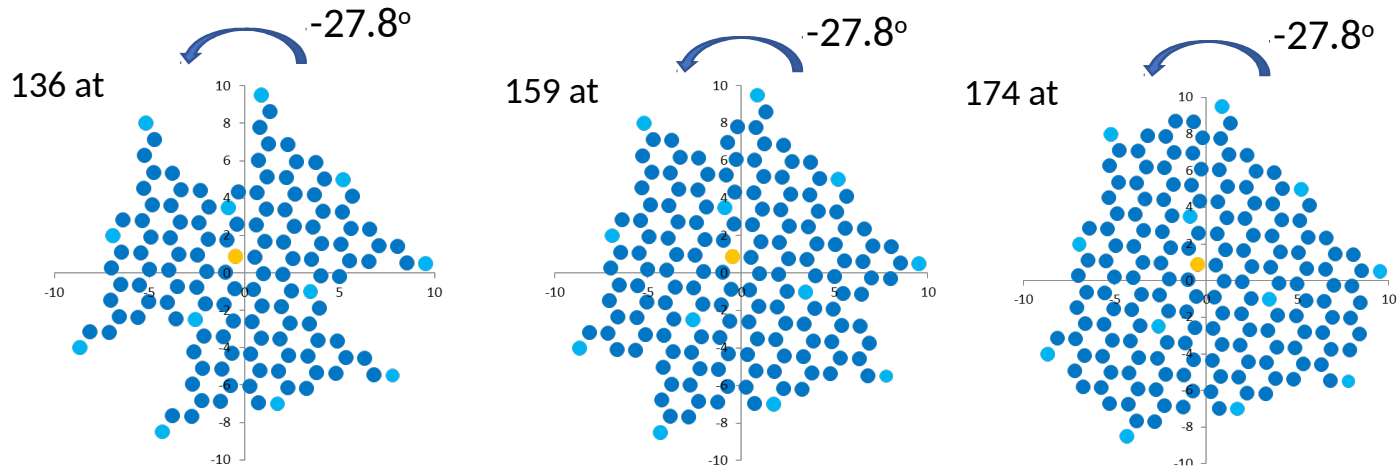


- Growth toward „pale blue” atoms stabilizes 27.8°
- Growth in other direction may diminishes metastability at 27.8° as shown for 118 atoms



Larger structures at 27.8°

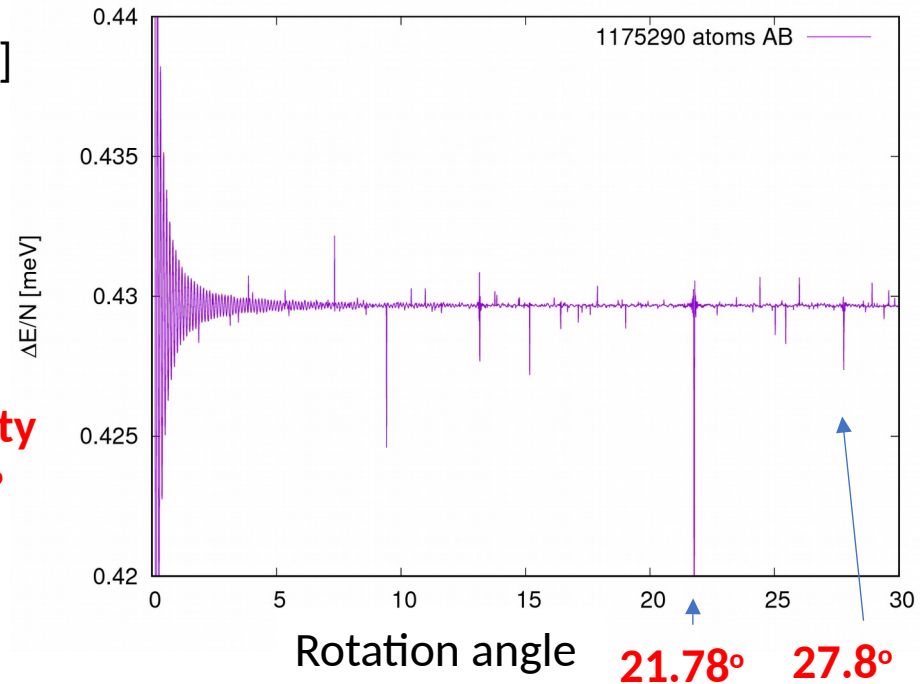
- Metastability may be preserved if „pale blue” atoms (at AB position after rotation) are on the tips of the Island with distinct triple symmetry 120°
- Preferred growth with triple symmetry 120°



LAMPS Simulation for 1 175 290 atoms

Kolmogorov and Crispy potential (K-C) [*]
gave results closer to experimental data
than Lenard-Jones potential

- Extremely narrow divergence of stability angles of structures twisted at 21.78° and 27.8°
- Possibly less than 0.2°



Simulated angles of stability compliant with angle of commensurate super-lattice structures by Castro [**]:

where (m,n) are pairs of co-prime numbers.

For example (m,n): $(1,1) - 21.787^\circ$, $(2,1) - 13.173^\circ$, $(3,1) - 9.43^\circ$, $(2,3) - 27.795^\circ$.

$$\cos\theta(m,n) = \frac{3m^2 + 3mn + n^2/2}{3m^2 + 3mn + n^2}$$

[*] A. N. Kolmogorov, V. H. Crespi, Registry-dependent interlayer potential for graphitic systems. Physical Review B, 71(23):235415, 2005

[**] A. H. Castro Neto J. M. B. Lopes dos Santos, N. M. R. Peres. Continuum model of the twisted graphene bilayer. Phys. Rev. B, 86:155449, 2012

Conclusions

- Growth of twisted Graphene layer starts after reaching some group of carbon atoms specific for given twist angle.
- Some atoms of twisted bilayer stabilize twisted configuration.
- Growth of twisted Graphene may diminish or enhance metastability of twisted configuration depending on growth direction
- Growth of twisted Graphene through preferential attaching atoms which stabilizes twisted configuration enhances metastability.
- The preferential growth of twisted bilayer with triple symmetry was simulated.

Thank you for your attention